# Trigonometry - Advanced problems

Sample plan, Henry Mord

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Problem	Solution 1	Solution 2	Solution 3
1. 1963 AHMSE Problem 34	$\checkmark$		
2. 1973 AHMSE Problem 17	$\checkmark$		
3. 1988 AHMSE Problem 13	$\checkmark$		
4. 1989 AHMSE Problem 14	$\checkmark$		
5. 2003 AMC Problem 21	$\checkmark$		
6. 2004 AMC Problem 21	$\checkmark$		
7. 2006 iTest Problem 9			
8. 2006 iTest Problem 17	$\checkmark$	$\checkmark$	
9. 2007 AMC Problem 17			
10. 2007 iTest Problem 17	$\checkmark$	$\checkmark$	$\checkmark$
11. 2008 iTest Problem 46	$\checkmark$		
12. 2017 AMC Problem 7	$\checkmark$		
13. 2020 AMC Problem 9			
14. 1993 U South Carolina Problem 10			
15. 1984 AIME Problem 13			

#### Source: Taken from www.artofproblemsolving.com

## Problems

## 1963 AHSME Problem 34

1. In triangle  $\triangle \text{DEF}$ , side  $d = \sqrt{3}$ , side  $e = \sqrt{3}$ , and side f > 3. Let t be the largest number such that the magnitude of the angle opposite side f exceeds t. Find t.

## 1973 AHSME Problem 17

2. If  $\alpha$  is an acute angle and  $\sin(\frac{\alpha}{2}) = \sqrt{\frac{x-1}{2x}}$ , then find  $\tan(\alpha)$ .

## 1988 AHSME Problem 13

3. If  $\sin(j) = 3\cos(j)$ , then what is  $\sin(j) \cdot \cos(j)$ ?

## 1989 AHSME Problem 14

4. What is  $\cot(10) + \tan(5)$ ?

## 2003 AMC Problem 21

5. An object moves 8 cm in a straight line from A to B, turns at an angle  $\beta$ , measured in radians and chosen from the interval  $(0, \pi)$ , and moves 5 cm in a straight line to C. What is the probability that AC < 7?

## 2004 AMC Problem 21

6. If  $\sum_{n=0}^{\infty} \cos^{2n} \delta = 4$ , what is the value of  $\cos 2\delta$ ?

#### 2006 iTest Problem 9

7. If  $\sin(x) = -\frac{5}{13}$  and x is in the third quadrant, what is the absolute value of  $\cos(\frac{x}{2})$ ?

#### 2006 iTest Problem 17

8. Let  $\sin(2x) = \frac{1}{7}$ . Find the numberical value of  $\sin(x)\sin(x)\sin(x)\sin(x)+\cos(x)\cos(x)\cos(x)\cos(x)$ 

## 2007 AMC Problem 17

9. Suppose that  $\sin(a) + \sin(b) = \sqrt{\frac{5}{3}}$  and  $\cos(a) + \cos(b) = 1$ . What is  $\cos(a - b)$ ?

## 2007 iTest Problem 17

10. If x and y are acute angles such that  $x + y = \frac{\pi}{4}$  and  $\tan(y) = \frac{1}{6}$ , find the value of  $\tan(x)$ .

#### 2008 iTest Problem 46

11. Let S be the sum of all x in the interval  $[0, 2\pi)$  that satisfy  $\tan^2(x) - 2\tan(x)\sin(x) = 0$ . Compute  $\lfloor 10S \rfloor$ .

## 2017 AMC Problem 7

12. The functions  $\sin(x)$  and  $\cos(x)$  are periodic with least period  $2\pi$ . What is the least period of the function  $\cos(\sin(x))$ ?

## 2020 AMC Problem 9

13. How many solutions are there to the equation  $\tan(3x) = \cos(x/2)$  on  $[0, 2\pi]$ ?

#### 1993 U South Carolina Problem 10

14. What is  $\arcsin(\frac{1}{3}) + \arccos(\frac{1}{3}) + \arctan(\frac{1}{3}) + \arctan(\frac{1}{3})?$ 

#### 1984 AIME Problem 13

15. What is  $10 \cot[\cot^{-1}(3) + \cot^{-1}(7) + \cot^{-1}(13) + \cot^{-1}(21)]$ ?